

# Randomness and uncertainty in SBML

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2010 SBML Hackathon

Seattle, USA

1–4 May, 2010

# distrib

- `distrib` proposal based around old proposal (on [sbml.org](http://sbml.org/wiki) wiki) from Newcastle, implemented in BASIS/`gillespie2`
- Adds random numbers from various distributions to MathML subset used by SBML
- Proposal just defined additional `csymbols`, but other ways to do it
- Random numbers are useful for assigning initial values for parameters and species amounts, in event assignments, event delays and potentially for timed events (though care must be taken)

# Rationale

- Generally useful for describing uncertainty about parameters (especially reaction rate constants) and about initial amounts for species
- Actually a philosophical difference between a description of uncertainty and the mechanism of choosing a random number
- Old proposal didn't make that distinction — could be relevant for certain kinds of analysis (including parameter scans)
- `UniformRandom` also best way to describe **ranges** — defines the natural scale — eg. for parameter scans
- Must **not** use random numbers in rate laws or other structures that are evaluated continuously — leads to undefined behaviour of the model — but see later...

# Questions

- 1 Make a distinction between describing uncertainty with a random quantity and picking one?
- 2 How many distributions? Trade-off between generality and implementation burden
- 3 Include PMFs/PDFs/CDFs etc, as well as actual distributions
- 4 How to encode in XML/SBML? To be nice to tools which don't understand...

# Particle representations

- Describing uncertainty with standard distributions is insufficiently general and flexible for describing uncertainty in biological models — especially **joint** distributions and distributions arising from **Monte Carlo algorithms** — uncertainty often not in standard form
- Often better to represent joint distribution over uncertain parameters with a large number of realisations from the distribution
- Big table — columns represent variables (eg. parameters and species), and rows represent realisations
- Can sample from the joint distribution simply by picking a row
- Can also represent parameter designs and scans this way — again, possible distinction between uncertainty description and mechanism of sampling

# Benefits

- Very natural for use in conjunction with Monte Carlo algorithms for both **uncertainty analysis** and **parameter inference** (Bayesian, MCMC, or otherwise)
- The output from MCMC algorithms, representing **posterior uncertainty**, has to be represented this way, and represents **prior uncertainty** for the next experiment...
- We have implemented this representation in CaliBayes ([www.calibayes.ncl.ac.uk](http://www.calibayes.ncl.ac.uk)), using a simple XML format external to the SBML
- Semantics — every variable in the table has its SBML values over-ridden by values picked from rows of the table
- Better in SBML? Big files, often containing **millions** of values...

# UncertML

- Systems biologists are obviously not the only people who worry about the representation of uncertainty in data, parameters and computer experiments...
- Draft specification for **UncertML** [www.uncertml.org](http://www.uncertml.org)
- This covers essentially everything covered so far (and more), including representation of uncertainty using both algebraic distributions and particle representations
- Very heavy-weight specification — would seriously hinder implementation if we were to adopt it all
- More focused on representation of uncertainty than on sampling from random distributions

## Extrinsic noise

- Discrete stochastic simulators are typically concerned with “intrinsic noise” in gene expression due to discreteness of biomolecules
- However, many other sources of noise and heterogeneity in biological systems
- “Extrinsic noise” is often modelled by allowing reaction rate constants to vary randomly and continuously in time according to a stochastic process governed by a stochastic differential equation (SDE)
- As mentioned previously, you can **not** just add random numbers into rate laws — the models will “blow up”
- Need a mechanism for defining SDEs within SBML models to make this work



# Implications

- Actually very easy from the point of view of SBML and libSBML
- Essentially just need a new `stochasticRateRule` to replace the existing rate rule, that will allow the definition of SDEs
- However, there are very significant implications for tool support — will require simulator developers to be competent in numerical stochastic integration (not easy), and also users to be familiar with stochastic differential equation modelling
- Therefore important to keep this separate from other random package(s) — other stuff is easy to implement and very useful
- Actually possible to implement SDEs approximately and inefficiently using existing SBML and discrete stochastic simulators, but involves exceptionally ugly hacks...