

Spatial Modeling in SBML

Issues for Level 3

Jim Schaff
VCell Project

Interested Parties:

Steve Andrews,
Johan Elf,
Thierry Emonet,
Mathilde Foglieri,
Akira Funahashi,
Michael Hucka,
Nicolas Le Novere,
Karen Lipkow,
Mike Mc Collum,
Poul Nielsen,
Michael North,
Greg Peterson,
Andrzej Przekwas,
Emmanuele Raineri,
Wayne Rindone,
Takeshi Sakurada,
Vijay Saraswat,
Jim Schaff,
Luis Serrano,
Tom Shimizu,
Joel Stiles,
Koichi Takahashi,
Dominic Tolle,
Yann Dublanche,
purvis

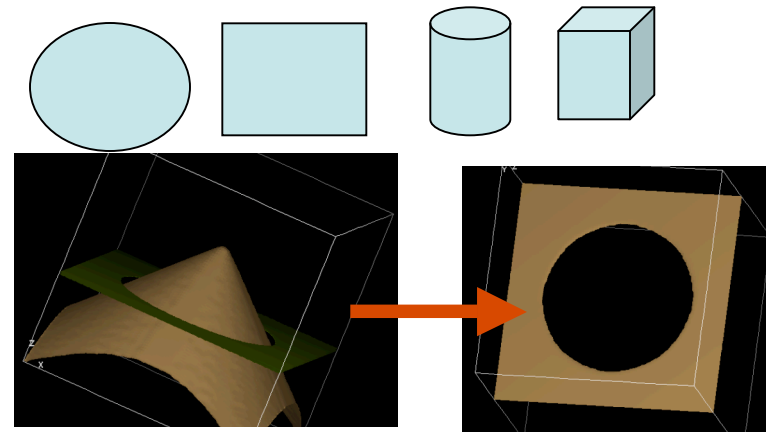
& others

Perspective (space vs. time)

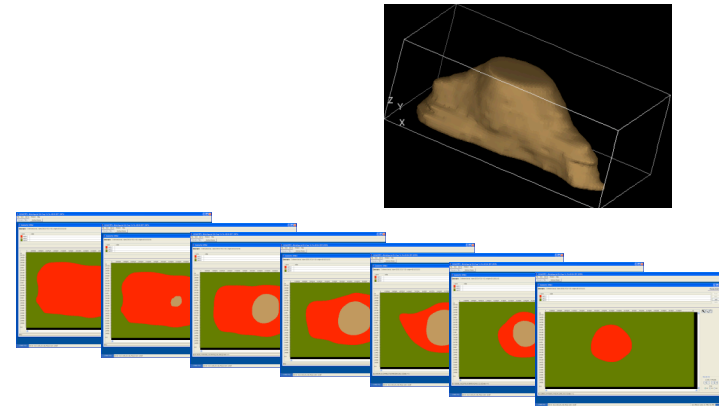
- Domain:
 - Time: $t = 0 \dots \text{Infinity}$; or ($-\text{Infinity} \dots \text{Infinity}$)
 - Space: defined by geometry (within bounding box?)
- Boundary Conditions:
 - Time: initial conditions, at $t = 0$, define value;
 - Space: at “edge” of geometry, define value, or flux, or periodic
- Discontinuities
 - Time: events – discontinuous jumps across time
 - Space: (spatial discontinuities – e.g. membranes)
- Discretization
 - Time: outside SBML (**tool problem**: “integrator time step”)
 - Space: outside SBML (**tool problem**: “mesh”)

Geometric Description

- Geometric Primitives with
 - Sphere (center, radius)
- Implicit inside/outside functions
 - $f(x,y,z) < 0$
 - level-set image \rightarrow [iso-surface, $f()=0$]



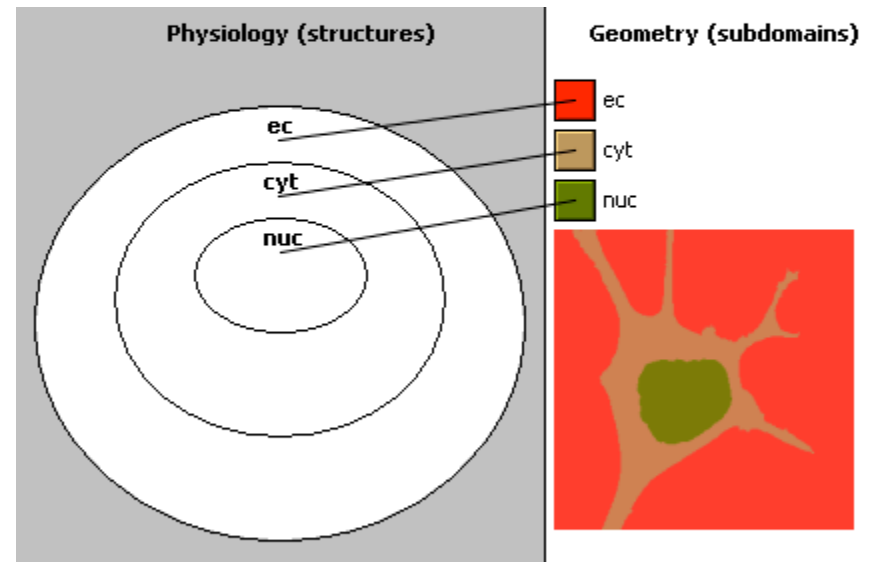
- Surface-based (polygonal)
- Segmented Images ?
 - Interpolate between slices
 - Need surface smoothing.



- Need common tools to convert between representations (libSPATIAL)
 - VCell ☺, ITK, VTK ...

Spatial Domains (and types)

- **Spatial domain types**
 - 1D, 2D (water-tight membranes), 3D Geometric definitions (not meshes)
 - Set of domains with same biology (**mapped from compartment**)
 - Annotated for anatomical description.
- Mapping of compartments to **spatial domain types**
 - Dimensions of geometry may be < 3D.
 - compartment “cytosol” mapped to **spatial domain type 2D**
 - IMPORTANT ASSUMPTIONS of missing 3rd dimension ... make explicit?
- Multiple instances **spatial domains** of spatial domain types.
 - e.g. multiple cells.
 - Bounding box?
- Topology of spatial domains
 - spatial ↔ nonspatial



Definition: Field

- Scalar valued function of position defined over a domain
 - Coordinate system (e.g. Cartesian, cylindrical, spherical)
 - $F(\mathbf{x}, t, \mathbf{p}, \mathbf{u})$ where
 - \mathbf{x} is a position (x,y,z) or (r,theta),
 - \mathbf{p} are parameters,
 - \mathbf{u} are variables,
 - t is time
 - image/lookup table (with basis function for interpolation)
- Examples:
 - Example 1: $\sin(x)*\cos(y)$ **explicit function of space**
 - Example 2: $\sin(x)*\cos(y)*t$ **explicit function of space and time**
 - Example 3: $(x<3)?(5):(0)$ **discontinuous function of space**
 - Example 4: $4*\text{calcium}$ **if “calcium” is a field**
 - Example 5: $\langle \text{image ref} \rangle, \text{scale, offset, size, bilinear interpolation}$ **image**

Spatially Resolved Species

- Initial Conditions:
 - PDE:
 - Concentration **FIELD**
 - Stochastic:
 - “Spatial Distribution Function” **FIELD**
 - List of initial positions (orientation?) for each individual
- Boundary Conditions:
 - PDE:
 - specify concentration **FIELD** (Dirichlet)
 - specify flux **FIELD** (Neumann)
 - periodic
 - Stochastic:
 - specify flux density probability **FIELD**
 - periodic

Spatially Resolved Species (continued)

- Diffusion Coefficient:
 - PDE:
 - **FIELD** - defined everywhere, could spatially vary.
(Could also be a function of local environment)
 - Stochastic:
 - **FIELD** – defined everywhere, could spatially vary.

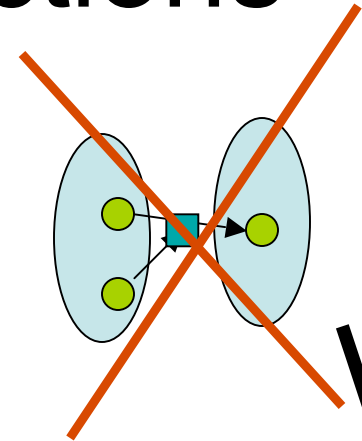
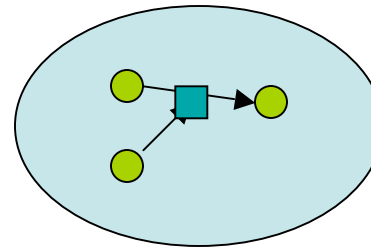
Spatially Resolved Reactions

- Reaction locations needed
- Volume Reactions:

- Reaction Rate:

- Deterministic: concentration per time
- Stochastic: function of true radii and “reactivity”???

- Reactants/Products/Modifiers in same volume

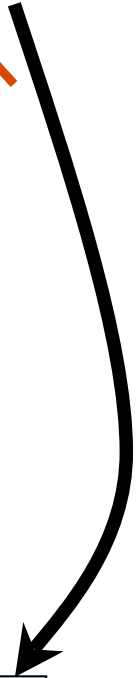
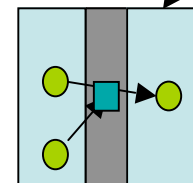
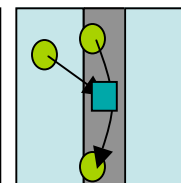
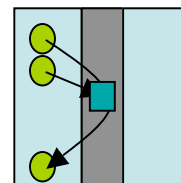
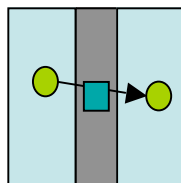
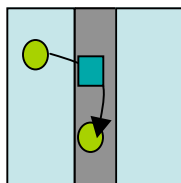


- Membrane Reactions:

- Reaction Rate:

- Deterministic: surface density per time (or flux density)
- Stochastic: function of true radii and “reactivity”???

- Reactants/Products/Modifiers in same “membrane” or adjacent volumes.



Related efforts

- Geometry Specifications:
 - CAD formats (e.g. IGES)
 - AVS/UCD, STL, VTK, ITK
- Spatial Modeling Languages
 - CellML/FieldML
 - VCML, ... other spatial simulation descriptions.
- Other Spatial Modeling Frameworks
 - lattice models
 - tissue/morphogenesis modeling
 - Agent-based populations of cells

Summary

- Geometry definition - not meshes
- Spatial distributions - functions or lookup tables
- All Reactions localized.
- Reactions rate in density/time for continuous
- Map compartments to SpatialDomainType
- Need shared geometry processing libraries (libSPATIAL)

- Spatial Proposal from community input.
- Start wiki at <http://ntcnp.org/> ... move to <http://sbml.org>